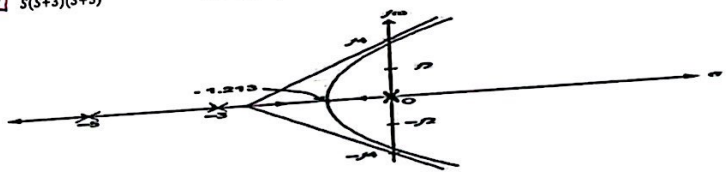




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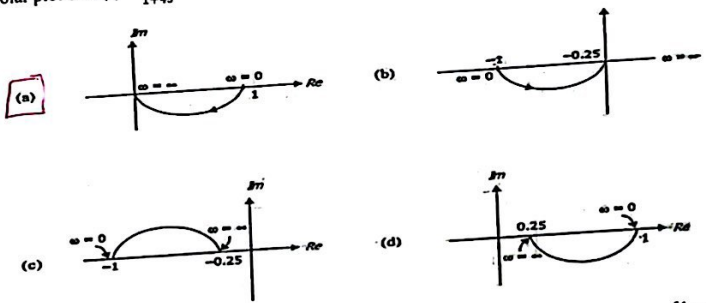
Q1: Choose the correct answer:

1. The root locus of a unity feedback system is shown in the following Figure. The open loop transfer function of the system is:
- a) $\frac{K}{s(s+3)(s+5)}$ b) $\frac{K}{s(s-3)(s-5)}$ c) $\frac{Ks}{(s+3)(s+5)}$ d) None of these [1 marks]



2. From a, the value of K at the break-away point is:
- a) 2.343 b) 4.632 c) 6.125 **d) 8.21** e) None of these [2 marks]
3. The angle of departure of the root locus from the pole ($s = -2+j$) for $G(s)H(s) = \frac{K}{(s+1)(s^2+4s+5)}$, is:
- a) -255 **b) -45** c) 45 d) None of these [2 marks]

4. The polar plot of $G(s) = \frac{1+s}{1+4s}$ for $0 \leq \omega \leq \infty$, is figure:



5. The term reset control refers to:
- a) Proportional controller b) derivative controller
c) Integral controller d) none of these [1 mark]
6. Effect of adding a pole to transfer function is:
- a) Pulling the root locus to the left **b) Pulling the root locus to the right** c) None of these

$$Q_3 \quad \boxed{9} \quad \frac{x_1}{x_2} = \frac{\boxed{1/2}}{s+10} \quad \frac{x_2}{u-x_3} = \frac{\boxed{1/2}}{s} \quad \frac{x_3}{x_1} = \frac{\boxed{1/2}}{s+1}$$

$$\dot{x}_1 = -10x_1 + 20x_2 \quad \dot{x}_2 = -x_3 - u \quad \dot{x}_3 = x_1 - x_3$$

$$y = x_1$$

$$\boxed{1} \quad \begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \\ \dot{x}_3 \end{bmatrix} = \begin{bmatrix} -10 & 20 & 0 \\ 0 & 0 & -1 \\ 1 & 0 & -1 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} + \begin{bmatrix} 0 \\ -1 \\ 0 \end{bmatrix} u$$

$$y = [1 \ 0 \ 0] \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} \quad \boxed{1/2}$$

$\boxed{5}$ marks

Q3 b

$$sI - A = \begin{bmatrix} s & -1 \\ 2 & s+3 \end{bmatrix} \quad \boxed{1}$$

$$|sI - A| = s^2 + 3s + 2 \quad \boxed{1}$$

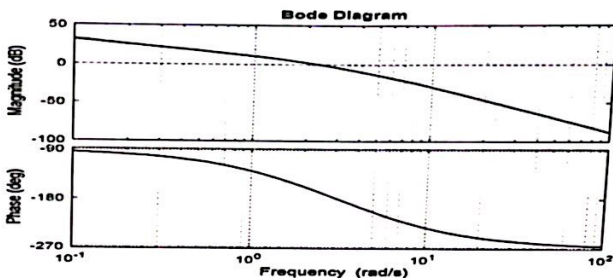
$\boxed{3}$ marks

$$(sI - A)^{-1} = \phi(s) = \begin{bmatrix} \frac{s+3}{(s+1)(s+2)} & \frac{1}{(s+1)(s+2)} \\ \frac{-2}{(s+1)(s+2)} & \frac{s}{(s+1)(s+2)} \end{bmatrix} \quad \boxed{1}$$



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7. The phase crossover frequency and gain crossover frequency from the following figure are:

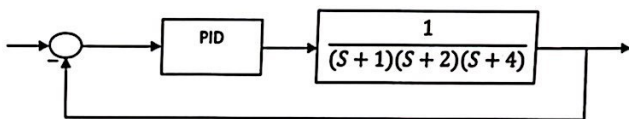


- a) 3.16 & 2.35 b) 10 & 1 c) 0.3 & 0.2 d) none of these [1 marks]

8. From 7, the system is:

- a) Stable b) unstable c) None of these [1 mark]

9. For the following system, the value of K_p that makes sustained oscillation will occur, is:



- a) 190 b) 90 c) 30 d) none of these [2 marks]

10. The gain margin of the following open loop transfer function $G(s)H(s) = 10 / S(S+1)(S+5)$, is:

- a) 11.3 b) 9.5db c) 7.5db d) None of these [3 marks]

11. The magnitude of the basic factor which, is a straight line with slope of 20 dB/decade and crossing the zero dB at $\omega=1$ is:

- a) $1/S$ b) S c) $(s+1)$ d) $1/(s+1)$ e) None of these

12. The eigen value of: $A = \begin{pmatrix} 0 & 1 \\ -12 & -7 \end{pmatrix}$, then determine if the system stable or unstable? [2 marks]

- a) -3 & -4 & unstable b) -3 & -4 & stable c) 3 & 4 & stable d) 3 & 4 & unstable e) None of these

13. Test the controllability of the system when: [2 marks]

$$A = \begin{pmatrix} 0 & 1 \\ 5 & -1 \end{pmatrix}, B = \begin{pmatrix} 2 \\ 1 \end{pmatrix}, \text{ and } C = (1 \ 1)$$

- a) Controllable b) Not controllable c) None of these

$$Q_2 \text{ a) } \frac{|G(s)H(s)|}{s = -2 + j\sqrt{2}} = \angle -30^\circ \quad [1]$$

6 marks

$$\text{let } a = 3 \quad \therefore b = 5.6 \quad [3]$$

$$k = 19.2 \quad [1]$$

$$k_{cr} = 1.92 \quad [1]$$

$$G_c(s) = 1.92 \cdot \frac{s+3}{s+5.6}$$

$$Q_2 \text{ b) } PM = 180 + \angle G(s)H(s)$$

$$40 = 180 + \angle G(s)H(s)$$

$$\angle G(s)H(s) = -140 \quad [1]$$

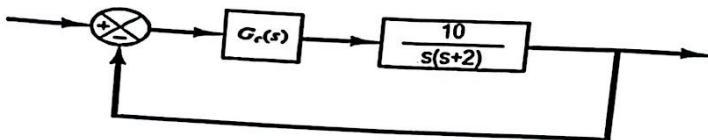
5 marks

$$\omega_{gc} = 1.678 \quad [2]$$

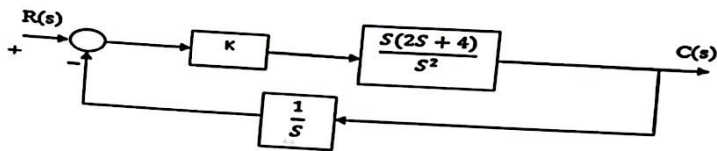
$$\therefore k = 0.541 \quad [2]$$

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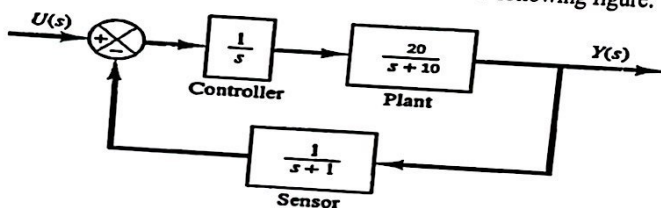
Q2: a) For the following system, Design a lead compensator such that the dominant closed loop poles located at $s = -2 \pm j\sqrt{12}$.



b) For the following control system, determine the value of the gain K such that the phase margin is 40° .



Q3: a) Obtain the state space model of the system shown in the following figure:



b) Find the resolvent matrix $\phi(s)$, of the given system:

$$\begin{pmatrix} \dot{x}_1 \\ \dot{x}_2 \end{pmatrix} = \begin{pmatrix} 0 & 1 \\ -2 & -3 \end{pmatrix} \begin{pmatrix} x_1 \\ x_2 \end{pmatrix} + \begin{pmatrix} 0 \\ 1 \end{pmatrix} u$$

Good Luck